

# HOPF ALGEBRA

**HOPF ALGEBRA** IS A FASCINATING AND EXTENSIVE TOPIC WITHIN THE REALM OF ALGEBRA, BRIDGING THE GAP BETWEEN ALGEBRAIC STRUCTURES AND TOPOLOGY. THIS MATHEMATICAL FRAMEWORK IS CRUCIAL FOR UNDERSTANDING VARIOUS AREAS, INCLUDING ALGEBRAIC TOPOLOGY, QUANTUM GROUPS, AND REPRESENTATION THEORY. HOPF ALGEBRAS CAN BE VIEWED AS A GENERALIZATION OF GROUPS AND RINGS, WITH THE UNIQUE PROPERTIES THAT ALLOW THEM TO SERVE AS A UNIFYING CONCEPT ACROSS DIFFERENT MATHEMATICAL DISCIPLINES. IN THIS ARTICLE, WE WILL EXPLORE THE DEFINITION OF HOPF ALGEBRA, ITS KEY PROPERTIES, EXAMPLES, APPLICATIONS, AND ITS SIGNIFICANCE IN MODERN MATHEMATICS.

THIS DISCUSSION WILL PROVIDE A COMPREHENSIVE OVERVIEW THAT NOT ONLY DEFINES HOPF ALGEBRAS BUT ALSO DELVES INTO THEIR RICH STRUCTURE AND VARIOUS APPLICATIONS. WE WILL ALSO ADDRESS SOME OF THE COMMON QUERIES SURROUNDING THIS TOPIC IN THE FAQ SECTION.

- DEFINITION OF HOPF ALGEBRA
- KEY PROPERTIES OF HOPF ALGEBRAS
- EXAMPLES OF HOPF ALGEBRAS
- APPLICATIONS OF HOPF ALGEBRAS
- SIGNIFICANCE IN MATHEMATICS
- CONCLUSION

## DEFINITION OF HOPF ALGEBRA

HOPF ALGEBRA IS A STRUCTURE THAT SIMULTANEOUSLY EXHIBITS CHARACTERISTICS OF BOTH ALGEBRA AND COALGEBRA. FORMALLY, A HOPF ALGEBRA OVER A FIELD  $(K)$  IS A VECTOR SPACE  $(H)$  EQUIPPED WITH SEVERAL OPERATIONS: MULTIPLICATION, UNIT, COMULTIPLICATION, COUNIT, AND ANTIPODE. THESE OPERATIONS MUST SATISFY SPECIFIC AXIOMS THAT DEFINE THEIR INTERRELATIONS, MAKING HOPF ALGEBRAS A RICH AREA OF STUDY IN ABSTRACT ALGEBRA.

THE KEY OPERATIONS IN A HOPF ALGEBRA CAN BE DESCRIBED AS FOLLOWS:

- **MULTIPLICATION:** A BILINEAR MAP  $(m: H \times H \rightarrow H)$  THAT IS ASSOCIATIVE.
- **UNIT:** A LINEAR MAP  $(\eta: K \rightarrow H)$  THAT PROVIDES AN IDENTITY ELEMENT.
- **COMULTIPLICATION:** A COASSOCIATIVE MAP  $(\Delta: H \rightarrow H \otimes H)$  THAT ALLOWS FOR THE DECOMPOSITION OF ELEMENTS.
- **COUNIT:** A LINEAR MAP  $(\epsilon: H \rightarrow K)$  THAT ACTS AS A DUAL IDENTITY.
- **ANTIPODE:** A MAP  $(S: H \rightarrow H)$  THAT ACTS LIKE AN INVERSE UNDER THE MULTIPLICATION OPERATION.

THESE OPERATIONS INTERACT IN A MANNER THAT PRESERVES THE ALGEBRAIC STRUCTURE AND ALLOWS FOR THE EXPLORATION OF VARIOUS MATHEMATICAL PHENOMENA. THE INTERPLAY BETWEEN ALGEBRAIC AND COALGEBRAIC STRUCTURES IS A DEFINING FEATURE OF HOPF ALGEBRAS, MAKING THEM A CRITICAL SUBJECT IN MODERN MATHEMATICS.

# KEY PROPERTIES OF HOPF ALGEBRAS

HOPF ALGEBRAS POSSESS SEVERAL CRUCIAL PROPERTIES THAT DISTINGUISH THEM FROM OTHER ALGEBRAIC STRUCTURES. UNDERSTANDING THESE PROPERTIES IS VITAL FOR THEIR APPLICATION AND STUDY. SOME OF THE KEY PROPERTIES INCLUDE:

## 1. DUALITY

ONE OF THE MOST SIGNIFICANT ASPECTS OF HOPF ALGEBRAS IS THEIR DUALITY. THE NOTION OF DUALITY IN HOPF ALGEBRAS REFERS TO THE RELATIONSHIP BETWEEN A HOPF ALGEBRA AND ITS DUAL, WHICH IS ALSO A HOPF ALGEBRA. THIS DUALITY PROVIDES INSIGHT INTO THE REPRESENTATION THEORY AND CAN LEAD TO THE DISCOVERY OF NEW STRUCTURES.

## 2. GRADING

MANY HOPF ALGEBRAS CAN BE GRADED, MEANING THAT THEY CAN BE DECOMPOSED INTO A DIRECT SUM OF SUBSPACES, EACH CORRESPONDING TO A SPECIFIC DEGREE. THIS GRADING PLAYS A CRUCIAL ROLE IN THE REPRESENTATION THEORY OF HOPF ALGEBRAS, ALLOWING FOR THE CLASSIFICATION OF REPRESENTATIONS BY THEIR DEGREE.

## 3. THE ANTIPODE

THE ANTIPODE IS A UNIQUE FEATURE OF HOPF ALGEBRAS THAT PROVIDES AN ALGEBRAIC ANALOGUE OF INVERSES. THE EXISTENCE OF THE ANTIPODE ALLOWS FOR THE FORMULATION OF A CATEGORY OF HOPF ALGEBRAS, WHERE MORPHISMS CAN BE DEFINED IN TERMS OF THE OPERATIONS OF THE HOPF ALGEBRA.

# EXAMPLES OF HOPF ALGEBRAS

TO BETTER UNDERSTAND HOPF ALGEBRAS, EXAMINING SPECIFIC EXAMPLES CAN BE BENEFICIAL. SEVERAL WELL-KNOWN HOPF ALGEBRAS ILLUSTRATE THE DIVERSITY AND RICHNESS OF THE STRUCTURE:

## 1. GROUP ALGEBRAS

FOR A FINITE GROUP  $(G, \cdot)$ , THE GROUP ALGEBRA  $k[G]$  IS A CLASSIC EXAMPLE OF A HOPF ALGEBRA. THE OPERATIONS ON THIS ALGEBRA ARE DEFINED IN TERMS OF THE GROUP OPERATIONS, MAKING IT A FUNDAMENTAL BUILDING BLOCK IN THE STUDY OF HOPF ALGEBRAS.

## 2. FUNCTION ALGEBRAS

ALGEBRAS OF FUNCTIONS ON ALGEBRAIC GROUPS CAN ALSO BE STRUCTURED AS HOPF ALGEBRAS. THESE FUNCTION ALGEBRAS REFLECT THE GEOMETRIC PROPERTIES OF THE UNDERLYING GROUP AND ARE ESSENTIAL IN THE STUDY OF ALGEBRAIC GEOMETRY.

### 3. QUANTUM GROUPS

QUANTUM GROUPS ARE ANOTHER INTRIGUING EXAMPLE OF HOPF ALGEBRAS THAT ARISE IN THE CONTEXT OF QUANTUM PHYSICS AND NON-COMMUTATIVE GEOMETRY. THEY GENERALIZE TRADITIONAL GROUPS AND PROVIDE A FRAMEWORK FOR STUDYING SYMMETRIES IN QUANTUM MECHANICS.

## APPLICATIONS OF HOPF ALGEBRAS

HOPF ALGEBRAS FIND APPLICATIONS ACROSS VARIOUS FIELDS OF MATHEMATICS AND THEORETICAL PHYSICS. THEIR VERSATILITY ALLOWS THEM TO BE UTILIZED IN MULTIPLE CONTEXTS, INCLUDING:

### 1. ALGEBRAIC TOPOLOGY

IN ALGEBRAIC TOPOLOGY, HOPF ALGEBRAS ARE USED TO STUDY THE PROPERTIES OF TOPOLOGICAL SPACES. THEY PROVIDE TOOLS FOR UNDERSTANDING COHOMOLOGY RINGS AND CAN BE EMPLOYED IN THE ANALYSIS OF FIBER BUNDLES.

### 2. REPRESENTATION THEORY

REPRESENTATION THEORY BENEFITS SIGNIFICANTLY FROM THE STUDY OF HOPF ALGEBRAS, ESPECIALLY IN THE CONTEXT OF FINITE-DIMENSIONAL REPRESENTATIONS. THE STRUCTURE OF HOPF ALGEBRAS ALLOWS FOR THE CLASSIFICATION AND ANALYSIS OF REPRESENTATIONS IN A SYSTEMATIC WAY.

### 3. QUANTUM PHYSICS

IN QUANTUM PHYSICS, HOPF ALGEBRAS PLAY A ROLE IN THE FORMULATION OF QUANTUM GROUPS, WHICH MODEL SYMMETRIES IN QUANTUM MECHANICS. THEY HELP IN UNDERSTANDING THE MATHEMATICAL FRAMEWORK OF QUANTUM FIELD THEORY AND STRING THEORY.

## SIGNIFICANCE IN MATHEMATICS

HOPF ALGEBRAS HOLD A PROMINENT PLACE IN CONTEMPORARY MATHEMATICS DUE TO THEIR RICH STRUCTURE AND WIDE-RANGING APPLICATIONS. THEY SERVE AS A BRIDGE BETWEEN VARIOUS MATHEMATICAL DISCIPLINES, ALLOWING FOR THE TRANSFER OF CONCEPTS AND TECHNIQUES. THEIR STUDY HAS LED TO SIGNIFICANT ADVANCEMENTS IN UNDERSTANDING ALGEBRAIC STRUCTURES, REPRESENTATION THEORY, AND TOPOLOGICAL PROPERTIES OF SPACES.

MOREOVER, THE ONGOING RESEARCH IN HOPF ALGEBRAS CONTINUES TO UNCOVER NEW APPLICATIONS AND CONNECTIONS WITH OTHER AREAS, REINFORCING THEIR IMPORTANCE IN THE MATHEMATICAL LANDSCAPE.

## CONCLUSION

HOPF ALGEBRAS REPRESENT A PROFOUND AND INTRICATE AREA OF STUDY IN MATHEMATICS, INTERTWINING ALGEBRA, TOPOLOGY,

AND THEORETICAL PHYSICS. THEIR UNIQUE PROPERTIES, EXTENSIVE APPLICATIONS, AND RICH EXAMPLES SHOWCASE THEIR SIGNIFICANCE AND VERSATILITY. AS RESEARCH PROGRESSES, HOPF ALGEBRAS WILL UNDOUBTEDLY CONTINUE TO PLAY A CRUCIAL ROLE IN ADVANCING MATHEMATICAL KNOWLEDGE AND UNDERSTANDING.

## **Q: WHAT IS A HOPF ALGEBRA?**

A: A HOPF ALGEBRA IS A STRUCTURE THAT COMBINES ALGEBRAIC AND COALGEBRAIC PROPERTIES, CONSISTING OF A VECTOR SPACE EQUIPPED WITH OPERATIONS OF MULTIPLICATION, UNIT, COMULTIPLICATION, COUNIT, AND AN ANTIPODE, SATISFYING SPECIFIC AXIOMS.

## **Q: WHAT ARE THE MAIN PROPERTIES OF HOPF ALGEBRAS?**

A: THE MAIN PROPERTIES OF HOPF ALGEBRAS INCLUDE DUALITY, GRADING, AND THE EXISTENCE OF THE ANTIPODE, WHICH FACILITATES THE FORMULATION OF A CATEGORY OF HOPF ALGEBRAS.

## **Q: CAN YOU GIVE EXAMPLES OF HOPF ALGEBRAS?**

A: EXAMPLES OF HOPF ALGEBRAS INCLUDE GROUP ALGEBRAS, FUNCTION ALGEBRAS ON ALGEBRAIC GROUPS, AND QUANTUM GROUPS, EACH ILLUSTRATING DIFFERENT ASPECTS OF THE HOPF ALGEBRA STRUCTURE.

## **Q: HOW ARE HOPF ALGEBRAS USED IN ALGEBRAIC TOPOLOGY?**

A: IN ALGEBRAIC TOPOLOGY, HOPF ALGEBRAS ARE UTILIZED TO STUDY THE PROPERTIES OF TOPOLOGICAL SPACES, ESPECIALLY IN UNDERSTANDING COHOMOLOGY RINGS AND FIBER BUNDLES.

## **Q: WHAT IS THE SIGNIFICANCE OF THE ANTIPODE IN HOPF ALGEBRAS?**

A: THE ANTIPODE ACTS AS AN INVERSE IN HOPF ALGEBRAS, PROVIDING A CRITICAL FEATURE THAT ALLOWS FOR THE DEFINITION OF MORPHISMS AND THE STUDY OF REPRESENTATIONS WITHIN THE ALGEBRAIC STRUCTURE.

## **Q: HOW DO HOPF ALGEBRAS RELATE TO QUANTUM PHYSICS?**

A: IN QUANTUM PHYSICS, HOPF ALGEBRAS ARE INSTRUMENTAL IN THE STUDY OF QUANTUM GROUPS, WHICH MODEL SYMMETRIES IN QUANTUM MECHANICS, CONTRIBUTING TO THE MATHEMATICAL FRAMEWORK OF QUANTUM FIELD THEORY.

## **Q: WHAT ROLE DO HOPF ALGEBRAS PLAY IN REPRESENTATION THEORY?**

A: HOPF ALGEBRAS ARE ESSENTIAL IN REPRESENTATION THEORY AS THEY FACILITATE THE CLASSIFICATION AND ANALYSIS OF FINITE-DIMENSIONAL REPRESENTATIONS, ENRICHING THE UNDERSTANDING OF ALGEBRAIC STRUCTURES.

## **Q: ARE THERE ANY MODERN DEVELOPMENTS IN THE STUDY OF HOPF ALGEBRAS?**

A: YES, ONGOING RESEARCH IN HOPF ALGEBRAS CONTINUES TO REVEAL NEW APPLICATIONS AND CONNECTIONS, FURTHER ENHANCING THEIR IMPORTANCE IN MATHEMATICS AND RELATED FIELDS.

# **Hopf Algebra**

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**hopf algebra: Classical Hopf Algebras and Their Applications** Pierre Cartier, Frédéric Patras, 2021-09-20 This book is dedicated to the structure and combinatorics of classical Hopf algebras. Its main focus is on commutative and cocommutative Hopf algebras, such as algebras of representative functions on groups and enveloping algebras of Lie algebras, as explored in the works of Borel, Cartier, Hopf and others in the 1940s and 50s. The modern and systematic treatment uses the approach of natural operations, illuminating the structure of Hopf algebras by means of their endomorphisms and their combinatorics. Emphasizing notions such as pseudo-coproducts, characteristic endomorphisms, descent algebras and Lie idempotents, the text also covers the important case of enveloping algebras of pre-Lie algebras. A wide range of applications are surveyed, highlighting the main ideas and fundamental results. Suitable as a textbook for masters or doctoral level programs, this book will be of interest to algebraists and anyone working in one of the fields of application of Hopf algebras.

**hopf algebra: Hopf Algebras and Generalizations** Louis H. Kauffman, David E. Radford, Fernando José Oliveira Souza, 2007 Hopf algebras have proved to be very interesting structures with deep connections to various areas of mathematics, particularly through quantum groups. Indeed, the study of Hopf algebras, their representations, their generalizations, and the categories related to all these objects has an interdisciplinary nature. It finds methods, relationships, motivations and applications throughout algebra, category theory, topology, geometry, quantum field theory, quantum gravity, and also combinatorics, logic, and theoretical computer science. This volume portrays the vitality of contemporary research in Hopf algebras. Altogether, the articles in the volume explore essential aspects of Hopf algebras and some of their best-known generalizations by means of a variety of approaches and perspectives. They make use of quite different techniques that are already consolidated in the area of quantum algebra. This volume demonstrates the diversity and richness of its subject. Most of its papers introduce the reader to their respective contexts and structures through very expository preliminary sections.

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**hopf algebra: Hopf Algebras** Jeffrey Bergen, Stefan Catoiu, William Chin, 2004-01-28 This volume publishes key proceedings from the recent International Conference on Hopf Algebras held at DePaul University, Chicago, Illinois. With contributions from leading researchers in the field, this collection deals with current topics ranging from categories of infinitesimal Hopf modules and bimodules to the construction of a Hopf algebraic

**hopf algebra: New Directions in Hopf Algebras** Susan Montgomery, Hans-Jurgen Schneider, 2002-05-06 Hopf algebras have important connections to quantum theory, Lie algebras, knot and braid theory, operator algebras and other areas of physics and mathematics. They have been intensely studied in the past; in particular, the solution of a number of conjectures of Kaplansky from the 1970s has led to progress on the classification of semisimple Hopf algebras and on the structure

of pointed Hopf algebras. Among the topics covered are results toward the classification of finite-dimensional Hopf algebras (semisimple and non-semisimple), as well as what is known about the extension theory of Hopf algebras. Some papers consider Hopf versions of classical topics, such as the Brauer group, while others are closer to work in quantum groups. The book also explores the connections and applications of Hopf algebras to other fields.

**hopf algebra:** *Hopf Algebras and Their Generalizations from a Category Theoretical Point of View* Gabriella Böhm, 2018-11-01 These lecture notes provide a self-contained introduction to a wide range of generalizations of Hopf algebras. Multiplication of their modules is described by replacing the category of vector spaces with more general monoidal categories, thereby extending the range of applications. Since Sweedler's work in the 1960s, Hopf algebras have earned a noble place in the garden of mathematical structures. Their use is well accepted in fundamental areas such as algebraic geometry, representation theory, algebraic topology, and combinatorics. Now, similar to having moved from groups to groupoids, it is becoming clear that generalizations of Hopf algebras must also be considered. This book offers a unified description of Hopf algebras and their generalizations from a category theoretical point of view. The author applies the theory of liftings to Eilenberg-Moore categories to translate the axioms of each considered variant of a bialgebra (or Hopf algebra) to a bimonad (or Hopf monad) structure on a suitable functor. Covered structures include bialgebroids over arbitrary algebras, in particular weak bialgebras, and bimonoids in duoidal categories, such as bialgebras over commutative rings, semi-Hopf group algebras, small categories, and categories enriched in coalgebras. Graduate students and researchers in algebra and category theory will find this book particularly useful. Including a wide range of illustrative examples, numerous exercises, and completely worked solutions, it is suitable for self-study.

**hopf algebra:** *A Course on Hopf Algebras* Rinat Kashaev, 2023-04-12 This textbook provides a concise, visual introduction to Hopf algebras and their application to knot theory, most notably the construction of solutions of the Yang-Baxter equations. Starting with a reformulation of the definition of a group in terms of structural maps as motivation for the definition of a Hopf algebra, the book introduces the related algebraic notions: algebras, coalgebras, bialgebras, convolution algebras, modules, comodules. Next, Drinfel'd's quantum double construction is achieved through the important notion of the restricted (or finite) dual of a Hopf algebra, which allows one to work purely algebraically, without completions. As a result, in applications to knot theory, to any Hopf algebra with invertible antipode one can associate a universal invariant of long knots. These constructions are elucidated in detailed analyses of a few examples of Hopf algebras. The presentation of the material is mostly based on multilinear algebra, with all definitions carefully formulated and proofs self-contained. The general theory is illustrated with concrete examples, and many technicalities are handled with the help of visual aids, namely string diagrams. As a result, most of this text is accessible with minimal prerequisites and can serve as the basis of introductory courses to beginning graduate students.

**hopf algebra:** *Advances in Hopf Algebras* Jeffrey Bergen, Susan Montgomery, 2023-08-18 This remarkable reference covers topics such as quantum groups, Hopf Galois theory, actions and coactions of Hopf algebras, smash and crossed products, and the structure of cosemisimple Hopf algebras.

**hopf algebra:** *An Introduction to Hopf Algebras* Robert G. Underwood, 2011-08-28 With wide-ranging connections to fields from theoretical physics to computer science, Hopf algebras offer students a glimpse at the applications of abstract mathematics. This book is unique in making this engaging subject accessible to advanced undergraduate and beginning graduate students. After providing a self-contained introduction to group and ring theory, the book thoroughly treats the concept of the spectrum of a ring and the Zariski topology. In this way the student transitions smoothly from basic abstract algebra to Hopf algebras. The importance of Hopf orders is underscored with applications to algebraic number theory, Galois module theory and the theory of formal groups. By the end of the book, readers will be familiar with established results in the field and ready to pose research questions of their own.

**hopf algebra:** *Hopf Algebra* Sorin Dascalescu, Constantin Nastasescu, Serban Raianu, 2000-09-15 This study covers comodules, rational modules and bicomodules; cosemisimple, semiperfect and co-Frobenius algebras; bialgebras and Hopf algebras; actions and coactions of Hopf algebras on algebras; finite dimensional Hopf algebras, with the Nicholas-Zoeller and Taft-Wilson theorems and character theory; and more.

**hopf algebra:** *Fundamentals of Hopf Algebras* Robert G. Underwood, 2015-06-10 This text aims to provide graduate students with a self-contained introduction to topics that are at the forefront of modern algebra, namely, coalgebras, bialgebras and Hopf algebras. The last chapter (Chapter 4) discusses several applications of Hopf algebras, some of which are further developed in the author's 2011 publication, *An Introduction to Hopf Algebras*. The book may be used as the main text or as a supplementary text for a graduate algebra course. Prerequisites for this text include standard material on groups, rings, modules, algebraic extension fields, finite fields and linearly recursive sequences. The book consists of four chapters. Chapter 1 introduces algebras and coalgebras over a field  $K$ ; Chapter 2 treats bialgebras; Chapter 3 discusses Hopf algebras and Chapter 4 consists of three applications of Hopf algebras. Each chapter begins with a short overview and ends with a collection of exercises which are designed to review and reinforce the material. Exercises range from straightforward applications of the theory to problems that are devised to challenge the reader. Questions for further study are provided after selected exercises. Most proofs are given in detail, though a few proofs are omitted since they are beyond the scope of this book.

**hopf algebra: Algebra and Applications 2** Abdenacer Makhlouf, 2021-12-29 This book is part of *Algebra and Geometry*, a subject within the SCIENCES collection published by ISTE and Wiley, and the second of three volumes specifically focusing on algebra and its applications. *Algebra and Applications 2* centers on the increasing role played by combinatorial algebra and Hopf algebras, including an overview of the basic theories on non-associative algebras, operads and (combinatorial) Hopf algebras. The chapters are written by recognized experts in the field, providing insight into new trends, as well as a comprehensive introduction to the theory. The book incorporates self-contained surveys with the main results, applications and perspectives. The chapters in this volume cover a wide variety of algebraic structures and their related topics. Alongside the focal topic of combinatorial algebra and Hopf algebras, non-associative algebraic structures in iterated integrals, chronological calculus, differential equations, numerical methods, control theory, non-commutative symmetric functions, Lie series, descent algebras, Butcher groups, chronological algebras, Magnus expansions and Rota-Baxter algebras are explored. *Algebra and Applications 2* is of great interest to graduate students and researchers. Each chapter combines some of the features of both a graduate level textbook and of research level surveys.

**hopf algebra:** *Hopf Algebras and Quantum Groups* Stefaan Caenepeel, Freddy Van Oystaeyen, 2019-05-07 This volume is based on the proceedings of the Hopf-Algebras and Quantum Groups conference at the Free University of Brussels, Belgium. It presents state-of-the-art papers - selected from over 65 participants representing nearly 20 countries and more than 45 lectures - on the theory of Hopf algebras, including multiplier Hopf algebras and quantum g

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**hopf algebra: Quasi-Hopf Algebras** Daniel Bulacu, Stefaan Caenepeel, Florin Panaite, Freddy Van Oystaeyen, 2019-02-21 This self-contained book dedicated to Drinfeld's quasi-Hopf algebras takes the reader from the basics to the state of the art.

**hopf algebra: Hopf Algebras and Their Actions on Rings** Susan Montgomery, 1993-10-28 The last ten years have seen a number of significant advances in Hopf algebras. The best known is the introduction of quantum groups, which are Hopf algebras that arose in mathematical physics and now have connections to many areas of mathematics. In addition, several conjectures of

Kaplansky have been solved, the most striking of which is a kind of Lagrange's theorem for Hopf algebras. Work on actions of Hopf algebras has unified earlier results on group actions, actions of Lie algebras, and graded algebras. This book brings together many of these recent developments from the viewpoint of the algebraic structure of Hopf algebras and their actions and coactions. Quantum groups are treated as an important example, rather than as an end in themselves. The two introductory chapters review definitions and basic facts; otherwise, most of the material has not previously appeared in book form. Providing an accessible introduction to Hopf algebras, this book would make an excellent graduate textbook for a course in Hopf algebras or an introduction to quantum groups.

**hopf algebra: Groups, Rings, Lie and Hopf Algebras** , 2003-03-31 The volume is almost entirely composed of the research and expository papers by the participants of the International Workshop Groups, Rings, Lie and Hopf Algebras, which was held at the Memorial University of Newfoundland, St. John's, NF, Canada. All four areas from the title of the workshop are covered. In addition, some chapters touch upon the topics, which belong to two or more areas at the same time. Audience: The readership targeted includes researchers, graduate and senior undergraduate students in mathematics and its applications.

**hopf algebra: Groups, Rings, Lie and Hopf Algebras** Y. Bahturin, 2013-12-01 The volume is almost entirely composed of the research and expository papers by the participants of the International Workshop Groups, Rings, Lie and Hopf Algebras, which was held at the Memorial University of Newfoundland, St. John's, NF, Canada. All four areas from the title of the workshop are covered. In addition, some chapters touch upon the topics, which belong to two or more areas at the same time. Audience: The readership targeted includes researchers, graduate and senior undergraduate students in mathematics and its applications.

**hopf algebra: Algebras, Rings and Modules** Michiel Hazewinkel, Nadezhda Mikhaïlovna Gubareni, Vladimir V. Kirichenko, 2010 Presenting an introduction to the theory of Hopf algebras, the authors also discuss some important aspects of the theory of Lie algebras. This book includes a chapters on the Hopf algebra of symmetric functions, the Hopf algebra of representations of the symmetric groups, the Hopf algebras of the nonsymmetric and quasisymmetric functions, and the Hopf algebra of permutations.

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